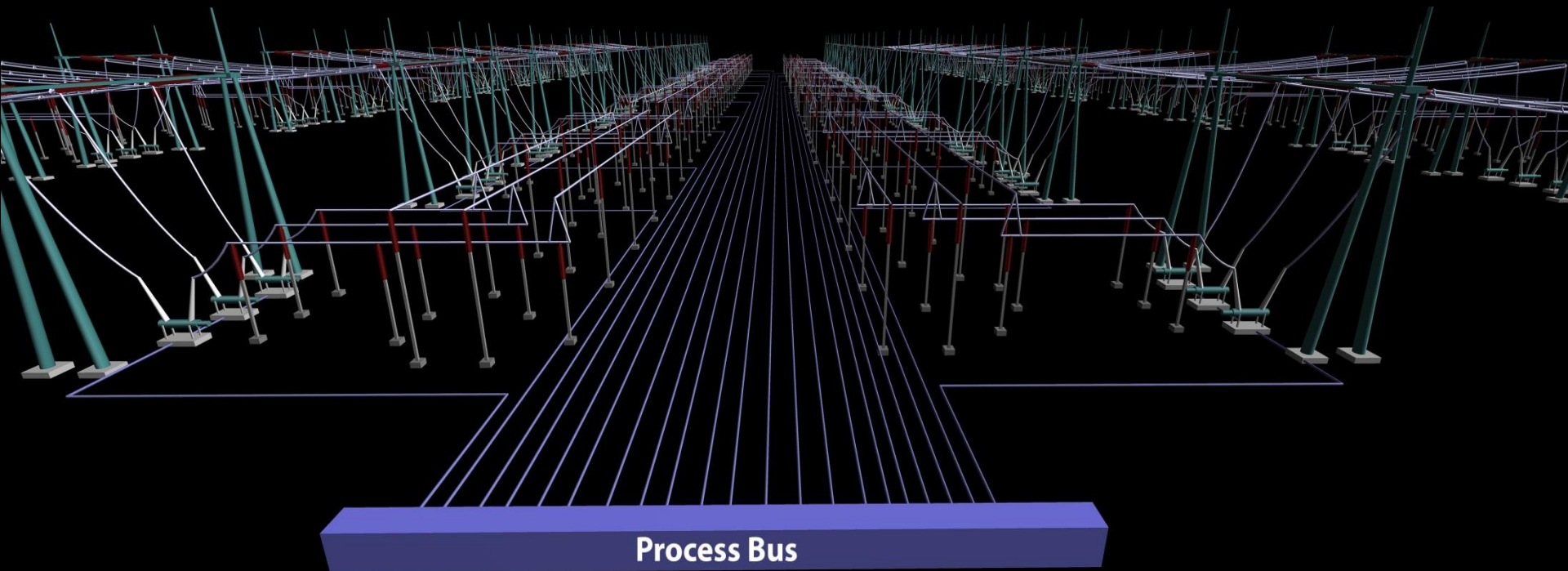


# Update On Distributed Dynamic State Estimators: Hybrid Inputs (PMUs, MUs, Numerical Relays) and Correction of Instrumentation Errors

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# Outline

## **Legacy State Estimators**

## **New Technologies: The Changing SCADA System**

Relays provide SCADA

Merging Units

GPS Synchronization

## **Distributed Dynamic State Estimators**

Integrated with Protection System

## **Error Correction**

## **Directions / Future Work**

# Legacy State Estimator

Introduced After the 1965 Blackout

Centralized State Estimator – Long Response (min)  
Model Biased State Estimator

## Power System SE: Basic Assumptions

- Positive Sequence Model
- P, Q, V measurement set
- Near-Simultaneous Measurements
- Single Frequency

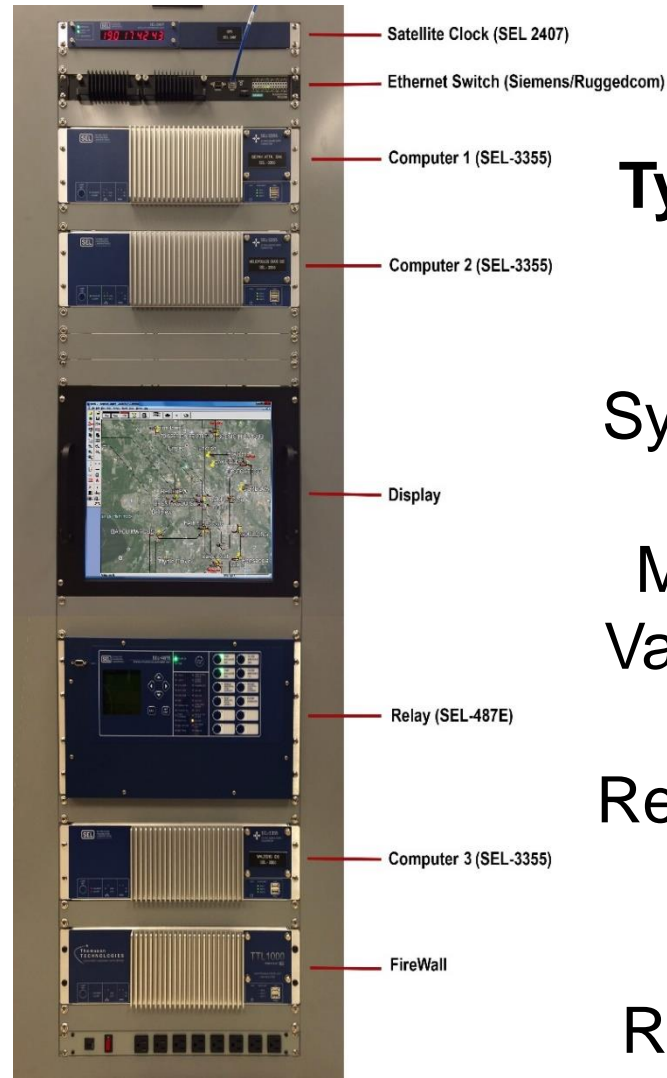
## Implications:

- Balanced Operation
- Symmetric Power System
- Biased SE
- Iterative Algorithm

Present Technologies  
Enable Removal of these  
Assumptions and  
Transition from Static to  
Dynamic State  
Estimators

# Present Technologies

Relays/Merging Units provide 3-Phase GPS Synchronized SCADA



## Typical Specs

GPS  
Synchronization

MU: Sampled  
Values at 80 s/c

Relays: Phasors  
at one s/c

Reality: Hybrid

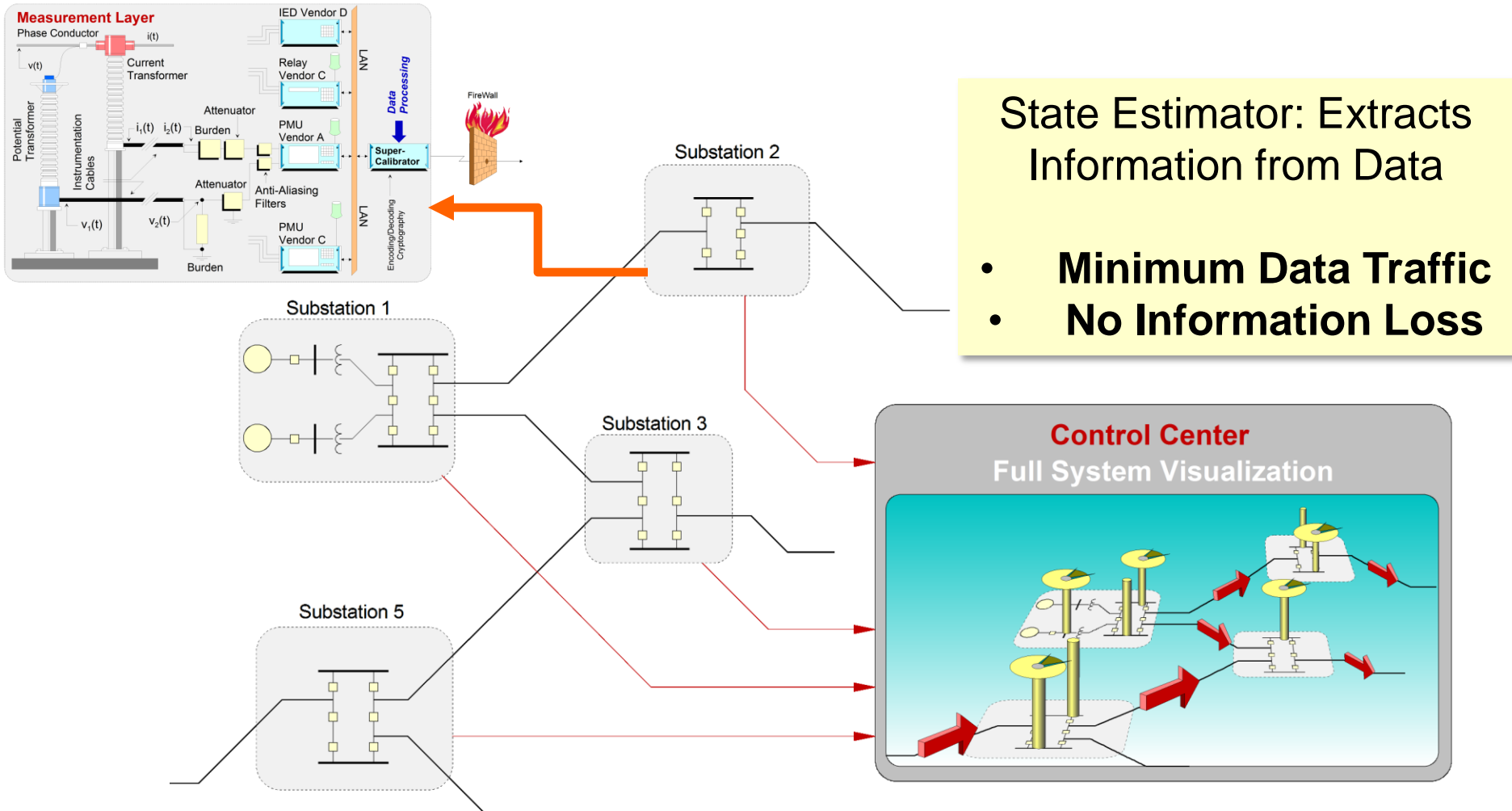
# Present Technology Enables Transition from Static State Estimators to Dynamic State Estimators.

- Dynamic State Estimators: Objective, Model (dynamic), Measurements
- Quasi-Dynamic State Estimators: Model Captures Slow Dynamics. Fast Electrical Dynamics are Ignored (Suitable for Operations).
- Dynamic State Estimators: Model Captures Slow and Fast Dynamics (Suitable for Protection).

# Distributed Quasi-Dynamic State Estimation

Substation Level SE → Synthesis of System Wide State at the Control Center  
Enabling Technology: GPS-Synchronized Measurements

## Substation Level State Estimation

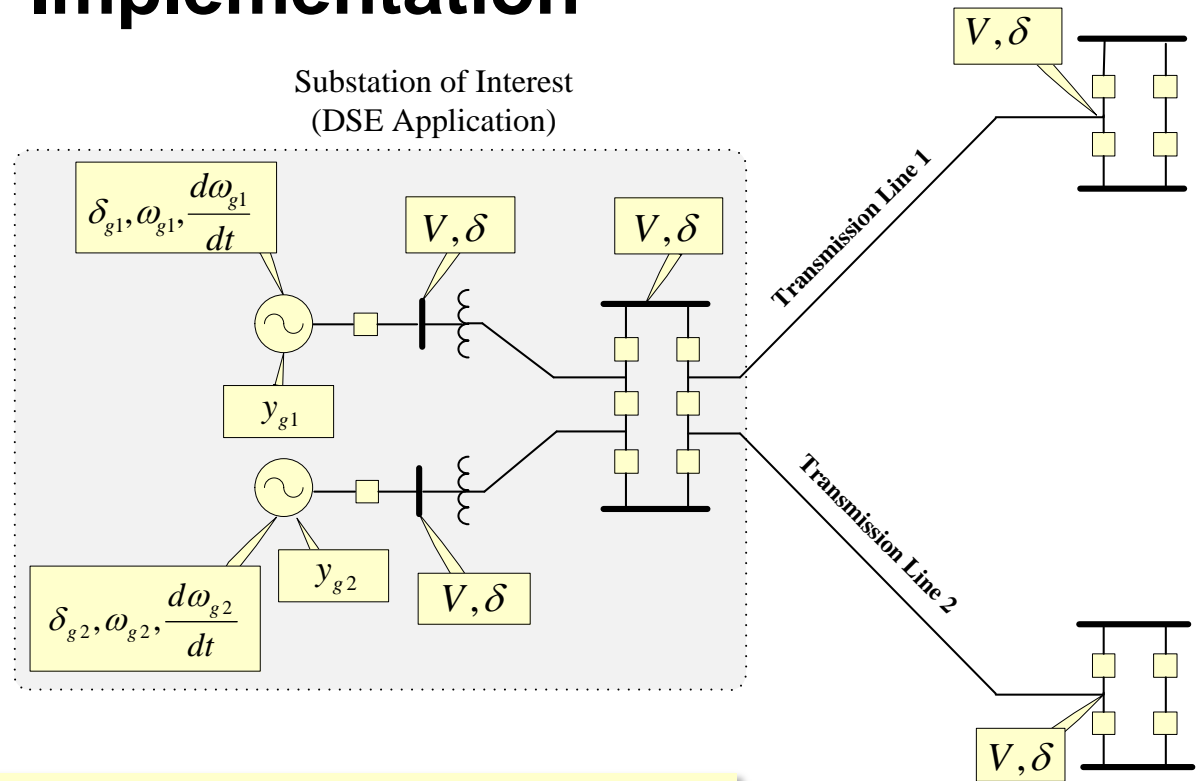


# Distributed Quasi-Dynamic State Estimation Implementation

The Estimator is Defined in Terms of:

- Model (Q-D)
- State
- Measurement Set
- Estimation Method

**Observability**  
**Redundancy**



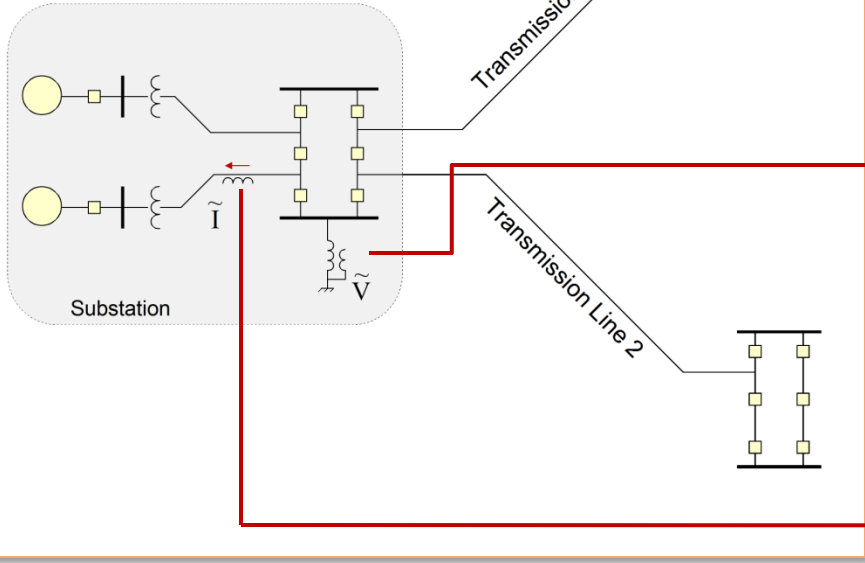
System is Represented with a Set of Differential Equations (DE)  
The Quasi-Dynamic State Estimator Fits the Streaming Data to the  
Quasi-Dynamic Model (QDE-slow dynamics) of the System

# Distributed SE Measurement Set

- Any Measurement at the Substation from Any IED  
(Relays, MU, Meters, FDR, PMUs, etc.)
- Data From at Least one GPS-Synchronized Device
- Augmentation of Data Set
  - Derived Measurements  
Based on Topology
  - Virtual Measurements  
Kirchoff's Current Law  
Model Equations
  - Pseudo-Measurements  
Missing Phase Measurements  
Neutral/Shield Current Measurement  
Neutral Voltage

# Object Oriented QSE

## Object Oriented Model



**Across (Voltage) Measurement:**

$$\tilde{z}_j(t) = \tilde{x}_j(t) + \eta_j$$

**Through (Current, Torque, etc.) Measurement:**

Measurement  $z_j(t)$  represents a quality associated with one row of the Object oriented model

$$\tilde{z}_j(t) = \text{row } k \text{ of Object Oriented Model} + \eta_j$$

$$\begin{bmatrix} \tilde{I}(t) \\ 0 \\ \tilde{I}(t_m) \\ 0 \end{bmatrix} = Y_{eq} \begin{bmatrix} \tilde{V}(t) \\ \tilde{Y}(t) \\ \tilde{V}(t_m) \\ \tilde{Y}(t_m) \end{bmatrix} + \begin{bmatrix} \tilde{V}^T(t) & \tilde{Y}^T(t) & \tilde{V}^T(t_m) & \tilde{Y}^T(t_m) \end{bmatrix} \cdot F_{eq} \cdot \begin{bmatrix} \tilde{V}(t) \\ \tilde{Y}(t) \\ \tilde{V}(t_m) \\ \tilde{Y}(t_m) \end{bmatrix} - B_{eq}$$

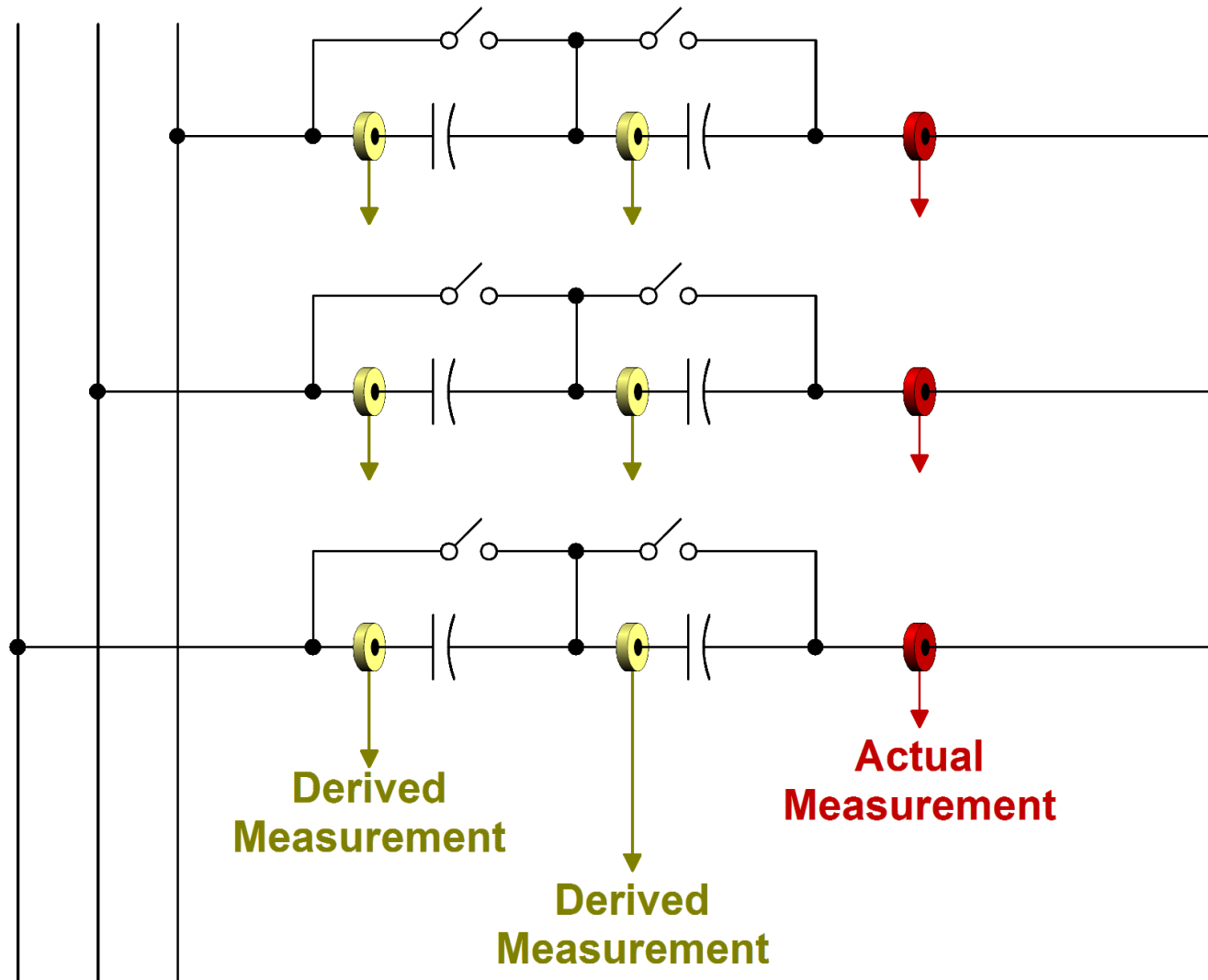
Row k

$$\text{where } B_{eq} = \sum_i A_i \cdot \begin{bmatrix} \tilde{V}(t-i \cdot h) \\ \tilde{Y}(t-i \cdot h) \end{bmatrix} + \sum_i B_i \cdot \begin{bmatrix} \tilde{I}(t-i \cdot h) \\ 0 \end{bmatrix} + C$$

QSE states are  
Phasors, Speed, etc

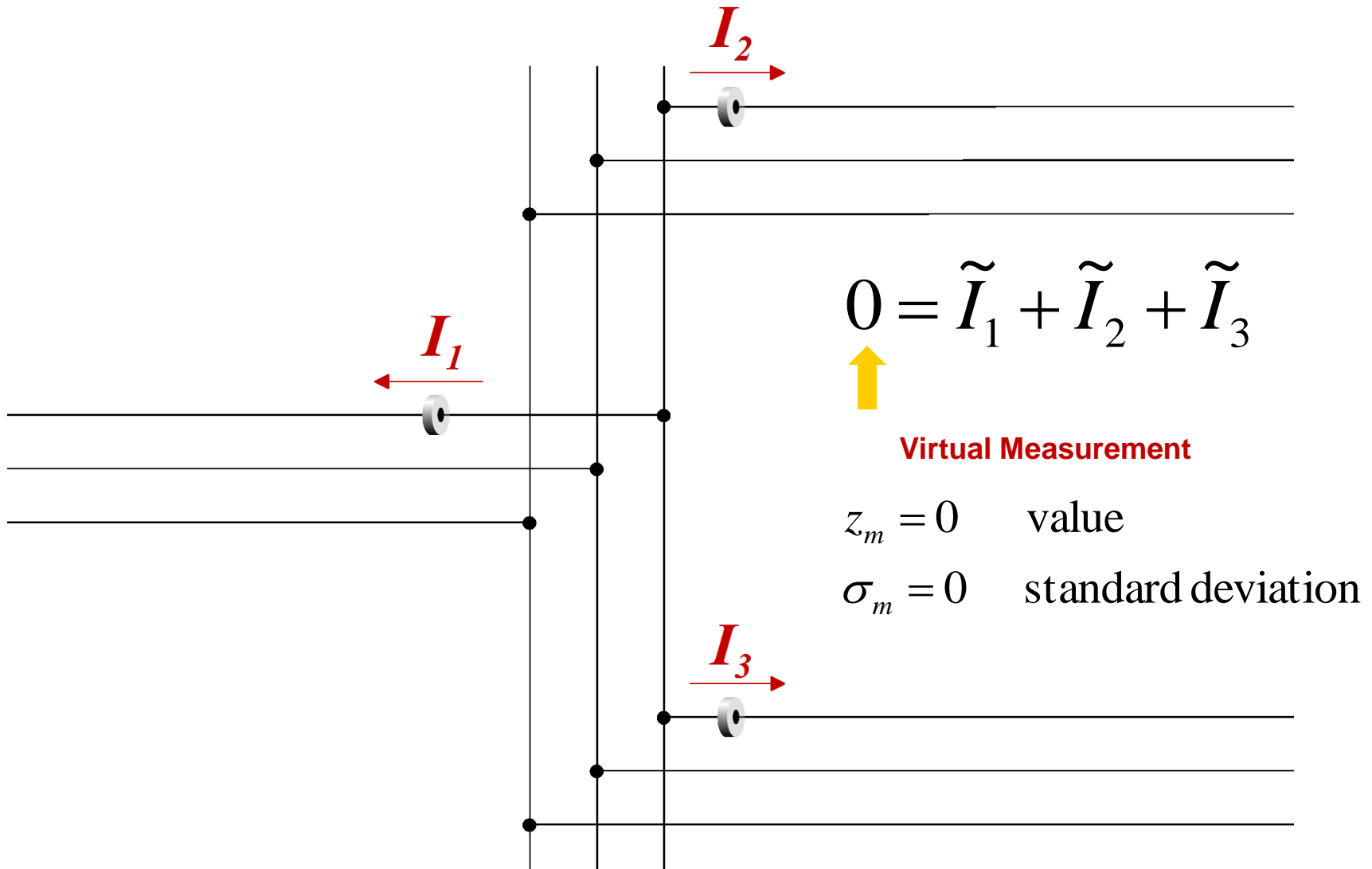
# Distributed State Estimation

## Derived Measurements - Examples



# Distributed State Estimation

## Virtual Measurements - Examples



# Distributed SE Measurement Set

## Non-Synchronized Measurements

Non-GPS Synchronized Relays provide phasors referenced on “phase A Voltage”.  
The phase A Voltage phase is ZERO.

The SuperC provides a reliable and accurate estimate of the phase A voltage phasor.

$$\tilde{A}_{sync} = \tilde{A}_{meas} e^{j\alpha}$$

$$\begin{aligned} \tilde{A}_{sync} &= \tilde{A}_{meas} e^{j\alpha} = \\ &A_{real} \cos \alpha - A_{imag} \sin \alpha + \\ &j(A_{real} \sin \alpha + A_{imag} \cos \alpha) \end{aligned}$$

$\alpha$  is a synchronizing unknown variable.

$\cos(\alpha)$  and  $\sin(\alpha)$  are unknown variables in the state estimation algorithm.

There is one  $\alpha$  variable for each non-synchronized relay.

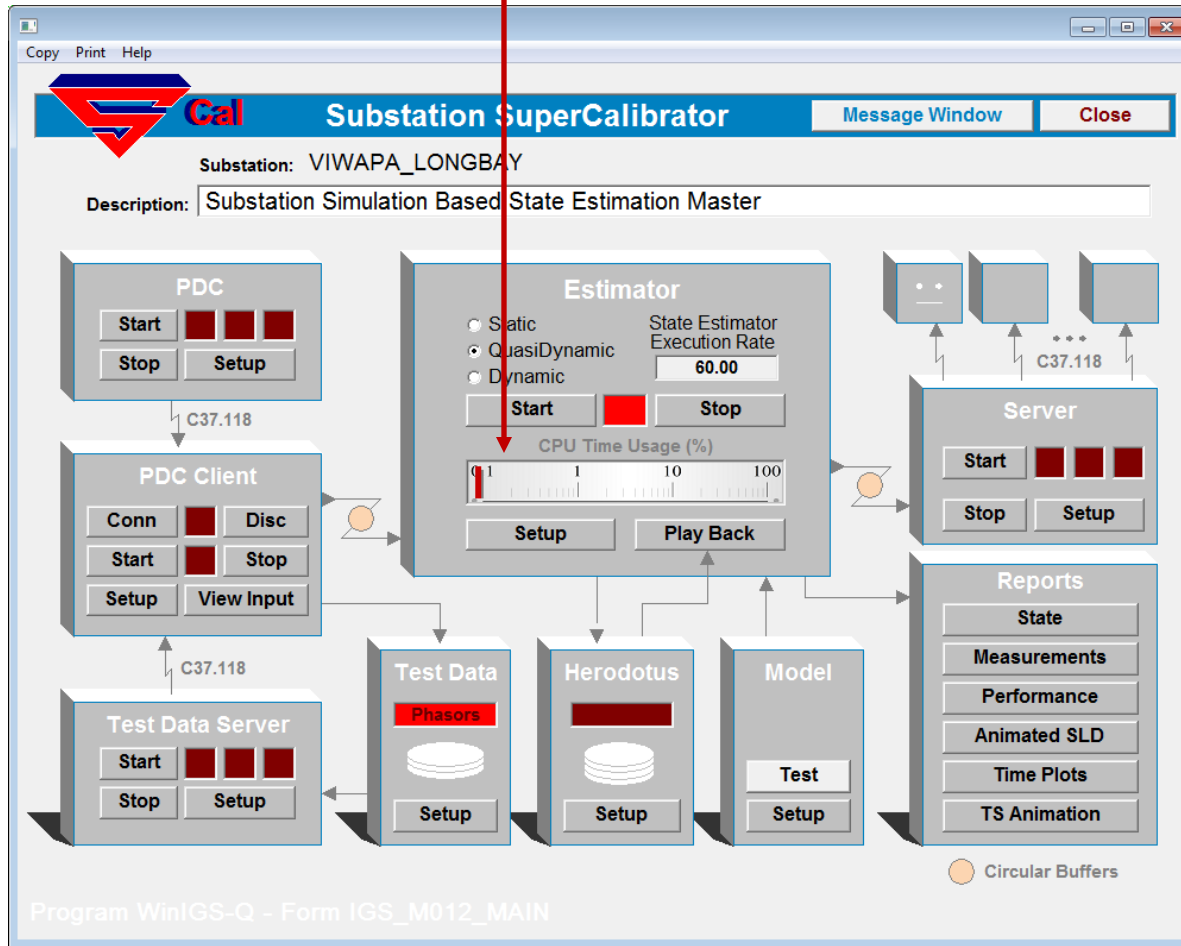
# Distributed Quasi-Dynamic SE Algorithms

- Unconstrained WLS,
- Constraint WLS,
- Extended Kalman Filter  
(Provides Model Uncertainty)

***Important Observation: Data and Model Fidelity is most important requirement for best performance***

# Performance Evolution: Distributed State Estimation

## Execution Time Monitor



CPU Time Usage Indicates in Real Time the Portion of the Time Used by the SE Calculations.

100% corresponds to the time between two successive SE computations.

Example: if SE is set to execute 60 times per second, then:

100%  $\rightarrow$  16.6 ms

# Implementation and Field Demonstrations

Snapshot of system:

- (a) visualization of system operation updated once per cycle
- (b) metric of data validity
- (c) displays of phasors and errors.

The image displays three software windows from the WinIGS-Q system:

- Top Left:** A 3D visualization of a power system with substations and transmission lines. The ground is green, and the sky is blue. Various components are labeled, such as 'SUBSTATION', 'BUS', and 'LINE'.
- Top Right:** The 'PMU Calibrator' window. It features a table of PMU data and a phasor plot.
 

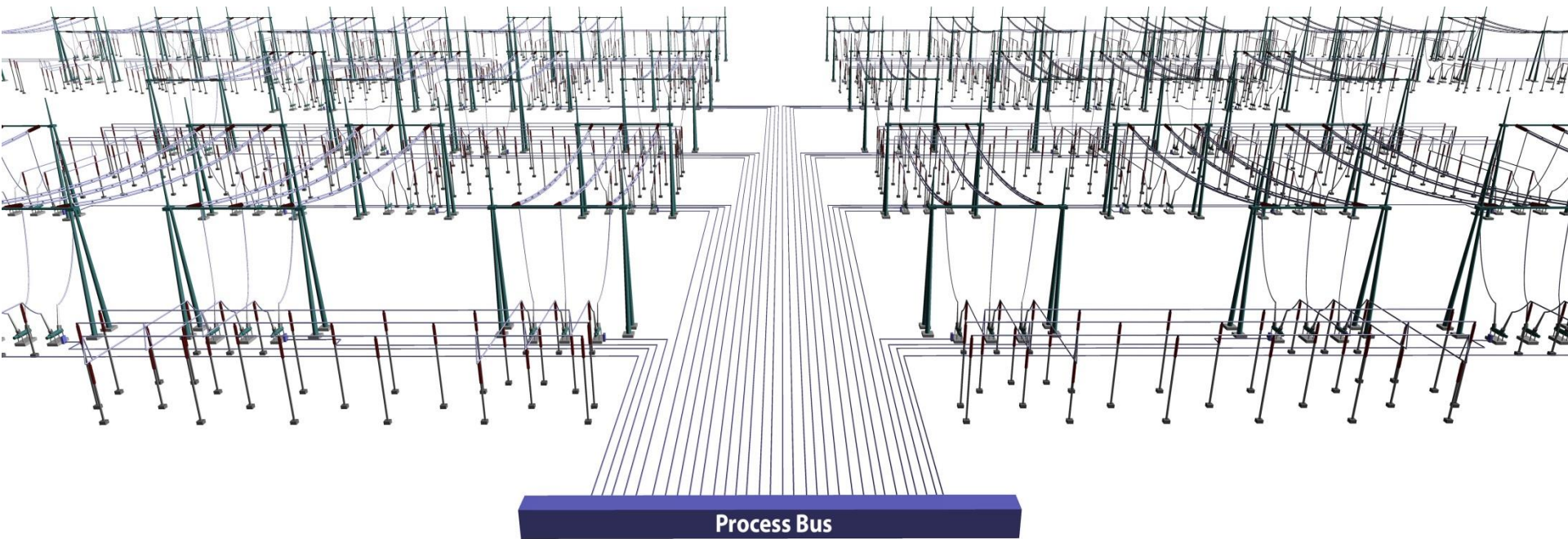
PMU	Channel	Value	Std Deviation	Plot
1	MU_PMU	V_SH-BUS8_AN	65.95 kV, 168.8 Deg	17.71 mDeg
2		V_SH-BUS8_BN	66.59 kV, 49.68 Deg	19.08 mDeg
3		V_SH-BUS8_CN	66.60 kV, -72.05 Deg	17.83 mDeg
10		V_SH-BUS11_CN	65.90 kV, 169.0 Deg	18.46 mDeg
11		V_SH-BUS11_BN	66.84 kV, 49.32 Deg	18.96 mDeg
12		V_SH-BUS11_CN	66.87 kV, -71.46 Deg	18.50 mDeg
16		V_SH-BUS5_AN	65.92 kV, 169.1 Deg	17.78 mDeg
17		V_SH-BUS5_BN	66.83 kV, 49.45 Deg	18.88 mDeg
18		V_SH-BUS5_CN	66.90 kV, -71.44 Deg	16.52 mDeg
22		V_SH-BUS14_AN	65.89 kV, 165.8 Deg	17.38 mDeg
23		V_SH-BUS14_BN	66.89 kV, 46.17 Deg	19.34 mDeg
24		V_SH-BUS14_CN	67.00 kV, -74.63 Deg	16.55 mDeg
28		N/A	65.87 kV, 165.8 Deg	18.01 mDeg
29		N/A	66.86 kV, 46.17 Deg	19.11 mDeg
30		N/A	66.99 kV, -74.63 Deg	16.62 mDeg
31	STATION A	V_SH-BUS14_AN	65.89 kV, 165.9 Deg	17.23 mDeg
32		V_SH-BUS14_BN	66.90 kV, 46.19 Deg	18.37 mDeg
33		V_SH-BUS14_CN	67.03 kV, -74.61 Deg	17.06 mDeg
34		N/A	5.331 V, -30.52 Deg	11.91 mDeg
35		N/A	5.987 V, -82.87 Deg	9.840 mDeg
36		N/A	2.771 V, -151.8 Deg	70.24 mDeg

 The phasor plot shows three vectors originating from the center. The largest vector is labeled (22) -2.9989. Other vectors are labeled (16) 0.2151 and (10) 0.1104. The plot has a scale from -1.00 to 1.00 and a frequency of F = 60.0150 Hz.
- Bottom Left:** The 'SuperCalibrator - Performance' window. It shows a graph of 'Parameter K' (y-axis, 0.1 to 10.0) versus 'Confidence Level' (x-axis, 0.00 to 100.0). The graph shows a red line that starts at approximately 0.2 and rises to 1.0 as the confidence level increases. Below the graph, there are fields for 'Confidence', 'D.O.F.' (set to 120), 'Iterations' (N/A), and 'Mismatch' (N/A). The timestamp is 12/01/2016, 18:49:09.066667.
- Bottom Right:** The 'Merging Unit Data Concentrator & PMU' window. It contains several sub-sections:
  - Concentrator Settings:** Includes 'View Data', 'Stop', and 'Start' buttons. Parameters include Sampling Rate (4800 s/sec), Max Latency (2000 samples), Main Buffer Size (8192 samples), and Plot Buffer Size (480 samples). Checkboxes for 'IED Active', 'Completeness Check', 'Time Domain Plot', 'Pause on Missing Data', 'Packet Reports', and 'Error Reports' are present.
  - Active Merging Units:** A table with columns for MU Identifier and Streaming status.
 

MU Identifier	Streaming
1 SIEMENSMU0101	●
2 SIEMENSMU0101	●
3 FLOSCMU04	●
4 MU320-SCENIC1	●
5 MU320-SCENIC2	●
  - Synchrophasers:** Includes 'Settings', 'Stop', and 'Start' buttons. Fields for 'PMU Name' (MU\_PMU) and 'F = 60.00414 Hz' are shown. A small phasor plot is also present.
  - Performance:** Shows 'Average Latency (%)' and 'Buffer Usage (%)' gauges.
  - Reference Clock:** Includes 'Synchronization' and 'Delta' (1.2870 sec) fields.
  - Error Counts:** Lists 'Smp Count 0', 'Too Late 0', 'Too Early 0', 'Out of Seq 0', and 'Smp Rate 0'.

# Data Integrity

## Instrumentation Channel Error Correction



# Effects of Input Data Accuracy

Quality of Data is Affected from:

- (a) *Instrumentation Channel Errors,*
- (b) *Hidden Failures and*
- (c) *Cyber data attacks.*

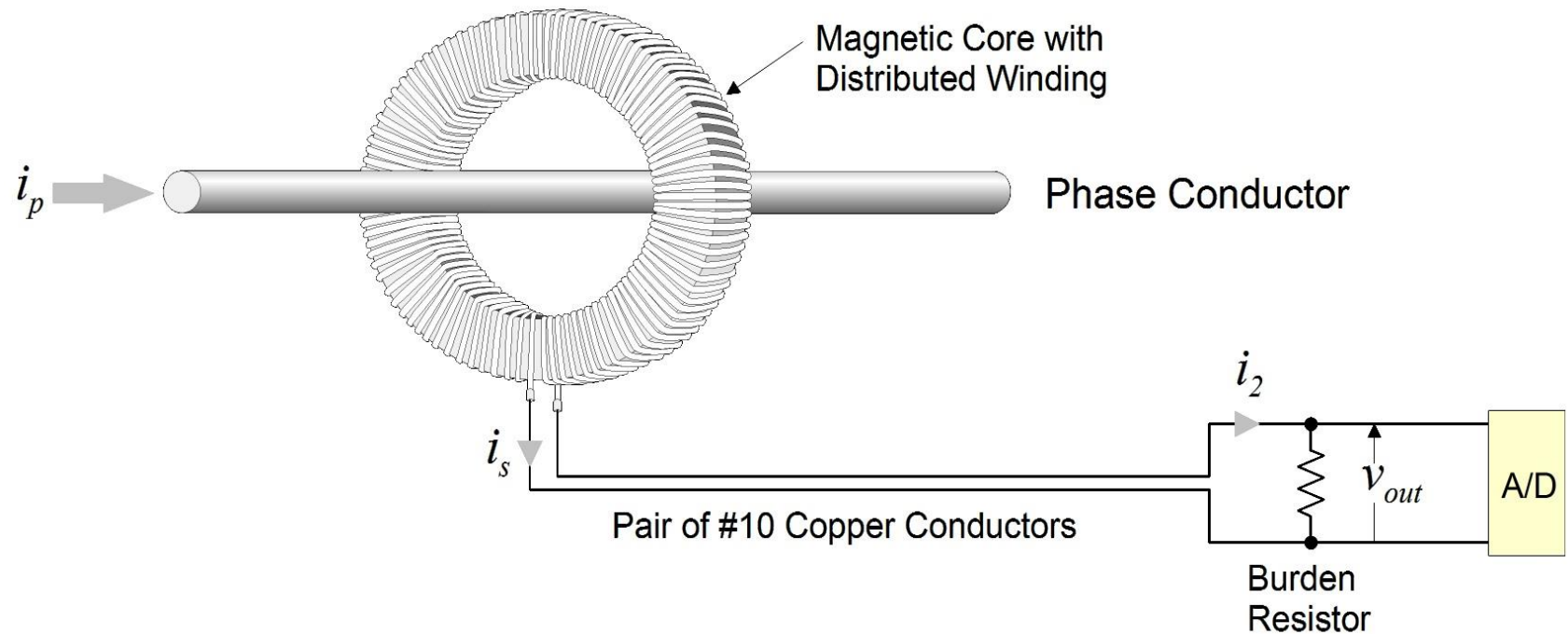
All Affect Performance of Protection and State Estimation.

Relays and merging units are becoming more accurate by using higher resolution in data acquisition and higher sampling rates.

Errors from instrumentation channels remain practically the same. Instrumentation channel errors have been much higher than the errors introduced by the data acquisition even in earlier generations of sensor less systems.

Merging Units offer a unique opportunity to perform error correction within a merging unit → MU provides corrected data in primary quantities.

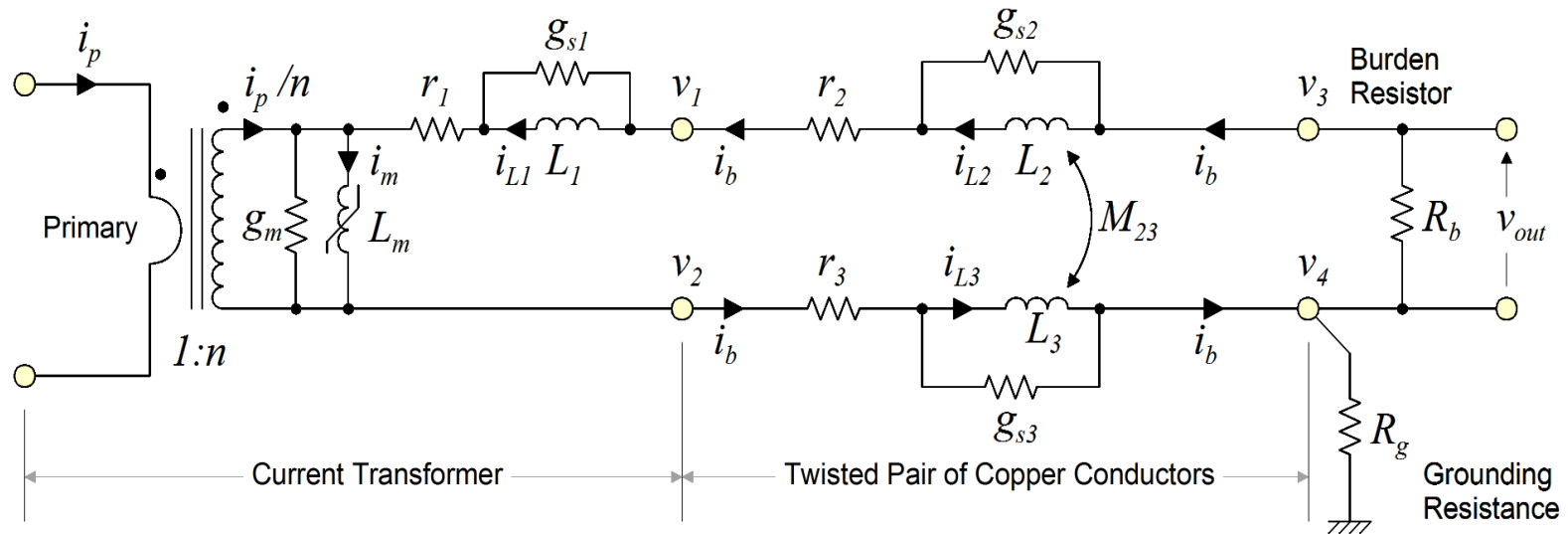
# Basic Question



- Given a measurement at the secondary of an instrumentation channel, can we extract the correct value of the primary quantity?
  - Can it be done on a sample by sample basis?

# Basic Approach to Error Correction

Construct the mathematical model of the instrumentation channel:  
Example CT Channel



Use actual measurements and augment with:

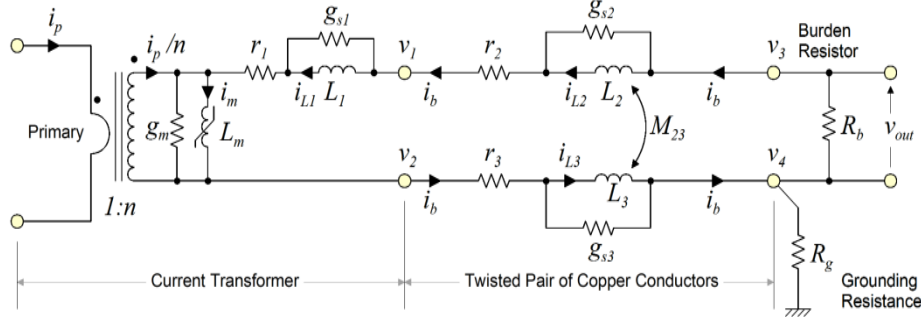
- (a) virtual measurements,
- (b) derived measurements, and
- (c) pseudo measurements

*Redundant Measurements.*

Perform dynamic state estimation → **Best Estimate Of Primary Current**

# Dynamic State Estimation

## CT Channel math Model



## Measurements

- Actual: Voltage or Current at Burden
- Add: -Virtual,  
-Derived, and  
-Pseudo-Measurements

Example Virtual Measurement: 
$$0 = -g_m e(t) - i_m(t) + \frac{1}{n} i_p(t) + i_{L_1}(t) + g_{s1} L_1 \frac{di_{L_1}(t)}{dt}$$

Example Derived Measurement: 
$$i_b^m(t) = i_{L_1}(t) + g_{s1} L_1 \frac{di_{L_1}(t)}{dt}$$

Example Pseudo Measurement: 
$$0^m = v_4(t)$$

21 Equations in 15 unknowns.

One of the unknowns is the Primary Current

States: 15

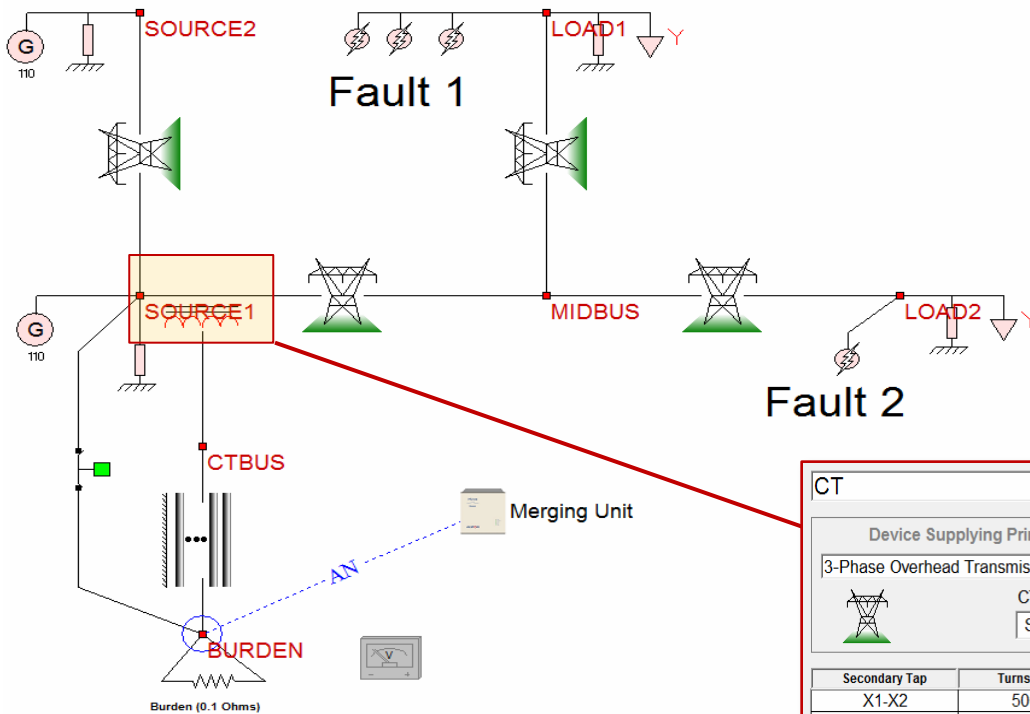
Actual Measurements: 1

Virtual Measurements: 14

Derived Measurements: 5

Pseudo measurements: 1

# Example System



## Example System Parameters

115-kV transmission system.

Current transformer on phase A

CT ratio is 800:5A

Error class: 10C100.

CT instrumentation cable: #10 copper

Instr. cable length: 96 meters

Burden resistance: 0.1  $\Omega$

## Current Transformer Parameters

**CT**

Device Supplying Primary Current  
3-Phase Overhead Transmission Line

CT on Terminal  
SOURCE1\_A

Secondary Tap	Turns Ratio
X1-X2	500:5
X1-X3	800:5
X1-X4	1000:5
X1-X5	1200:5
X1-X6	2000:5

Save

Secondary Voltage (Vrms) vs Magnetizing Current (Amps) graph

Log Axis

$k = 116$  A

$i(t) = i_0 \left| \frac{\lambda(t)}{\lambda_0} \right|^n \times \text{sgn}(\lambda(t))$

Exponent (n) = 11

Circuit Number: 1

CT Secondary Terminals: CTBUS\_A, CTBUS\_N

Error Class: C 5.00 % at 20 x Rated Current

Voltage Class: 50.00 Volts

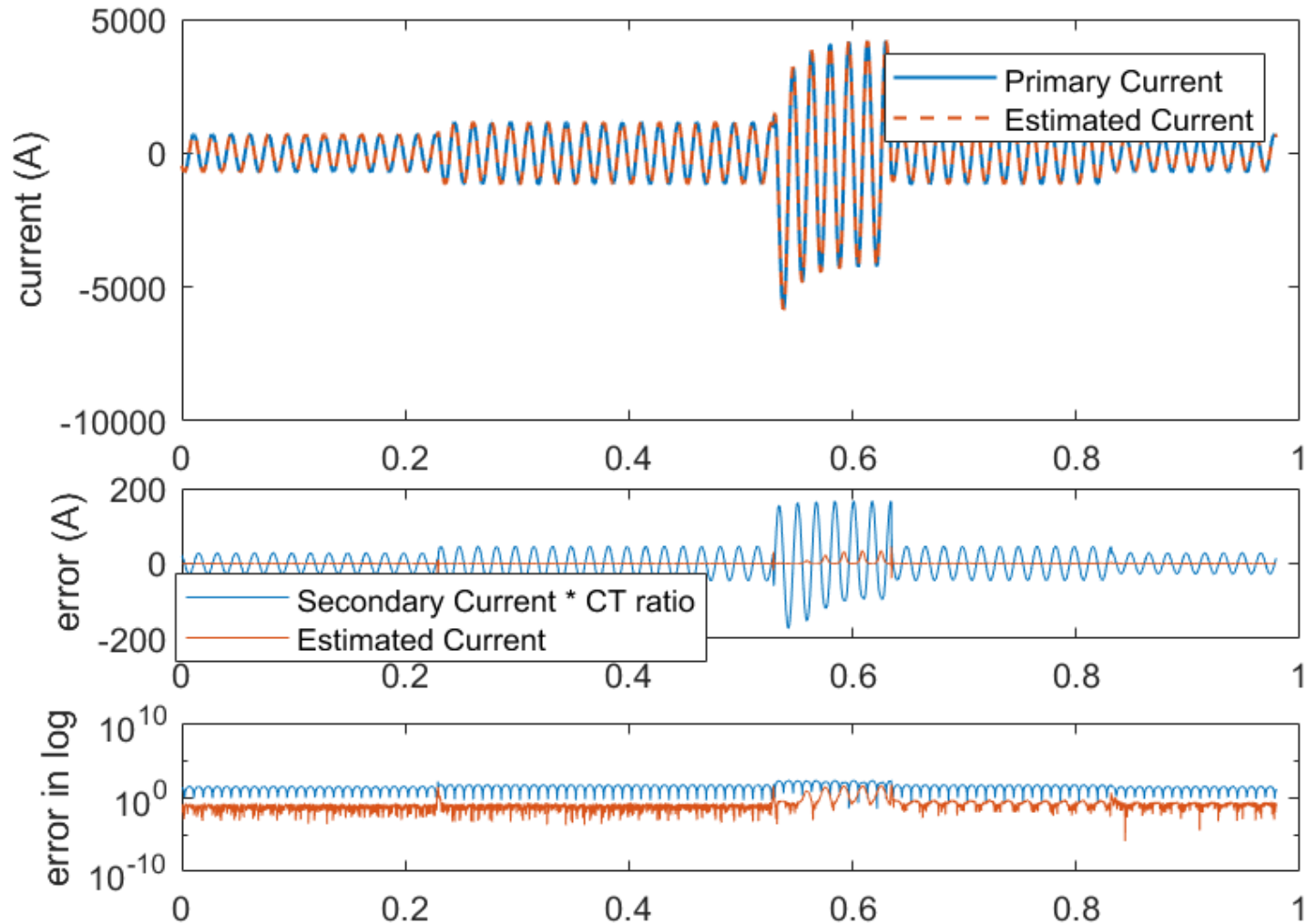
Tap Selection: X1-X6

Update  $i_0$

Match specified error class

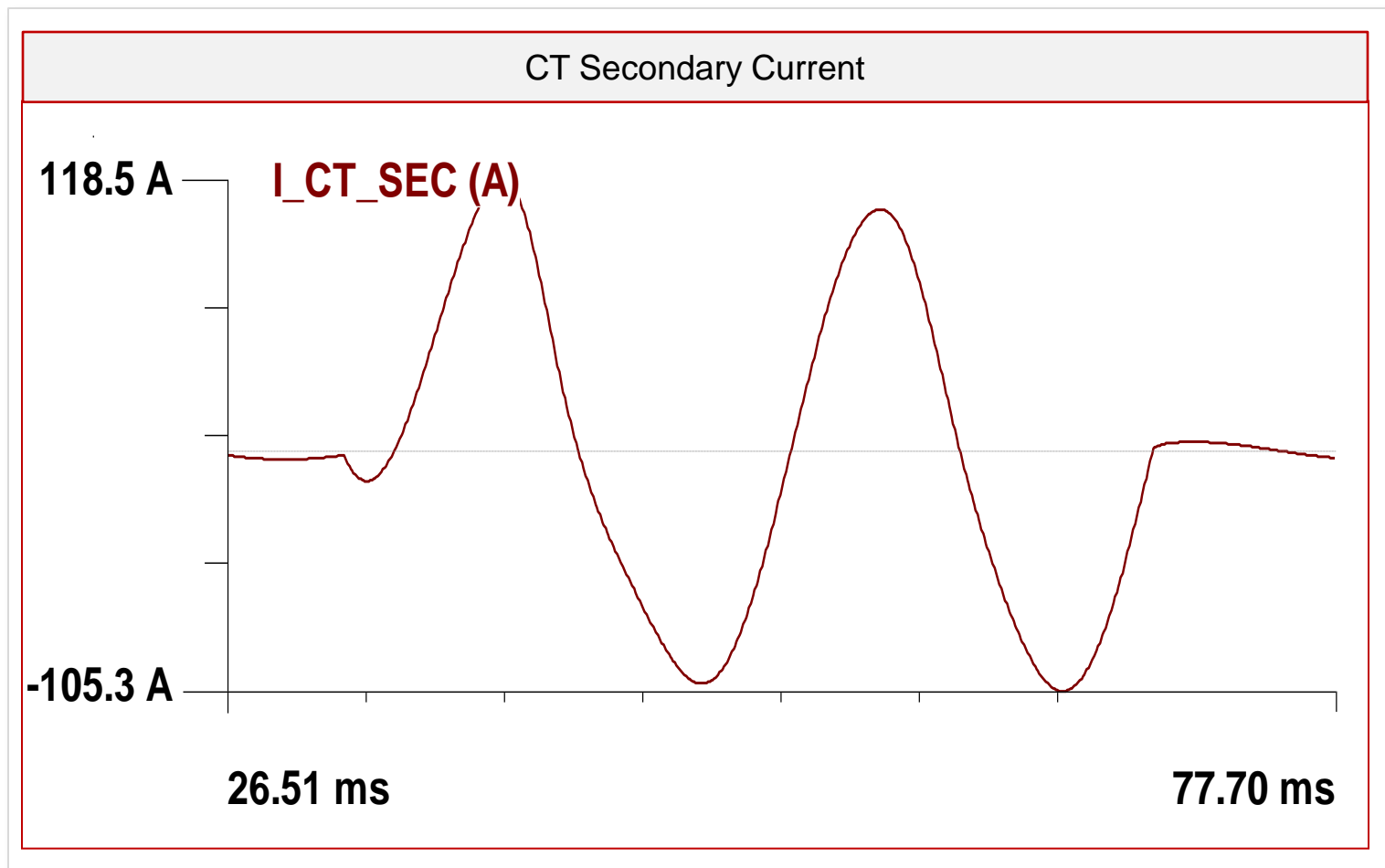
Selected Tap Parameters		Full Coil Parameters	
Primary Rating		2000.0	Amperes
Secondary Rating		5.0	Amperes
Coil Resistance	0.00500	0.00500	Ohms
Leakage Reactance	0.01000	0.01000	Ohms
Core Conductance	0.00100	0.00100	Siemens
Magnetizing Current ( $i_0$ )	6.09109	6.09109	Amperes

# Example System Results



# Example System Results – Mild CT Saturation

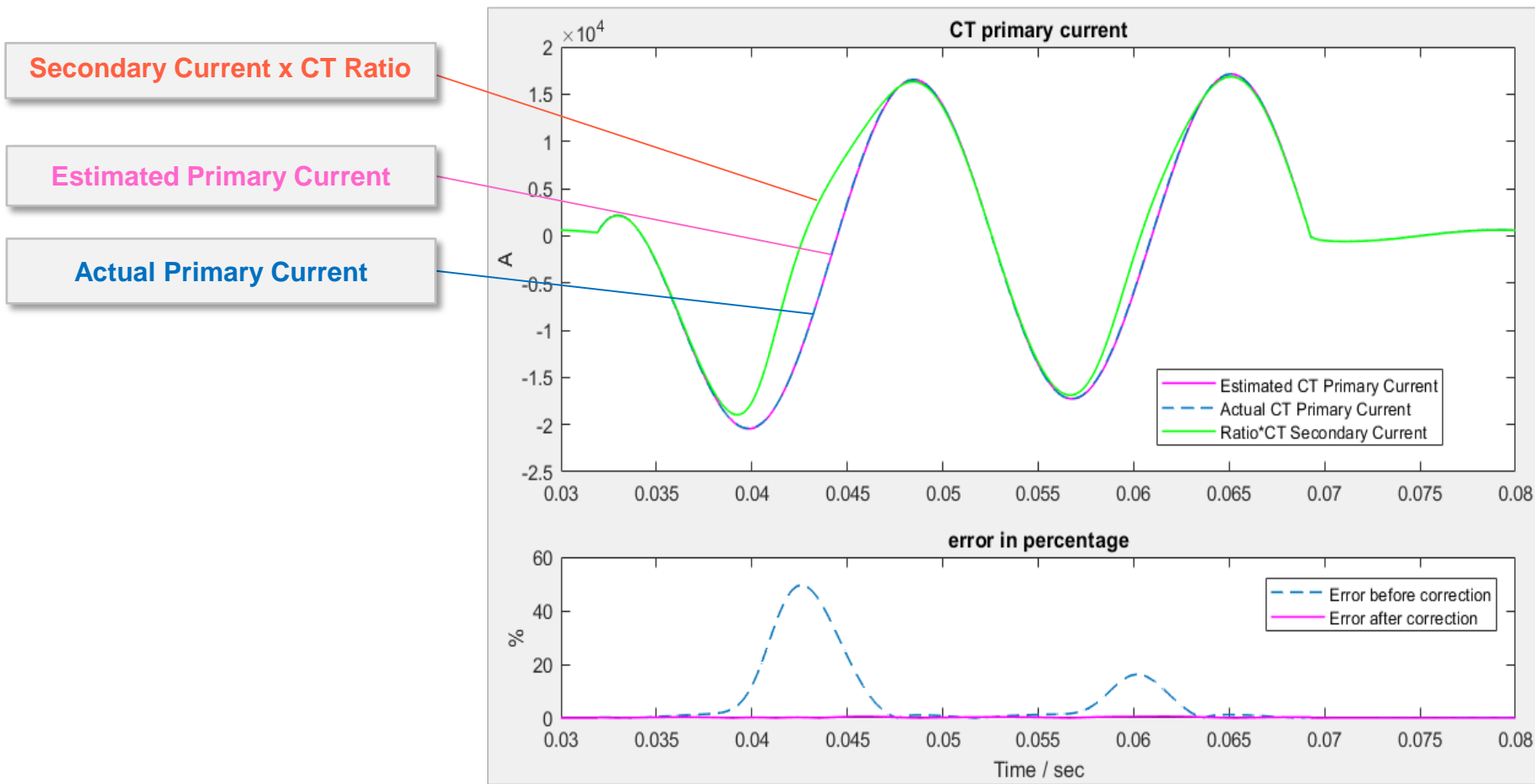
## Simulated CT Secondary Current Waveform



Phase A to ground fault at “MIDBUS”

# Example System Results – Mild CT Saturation

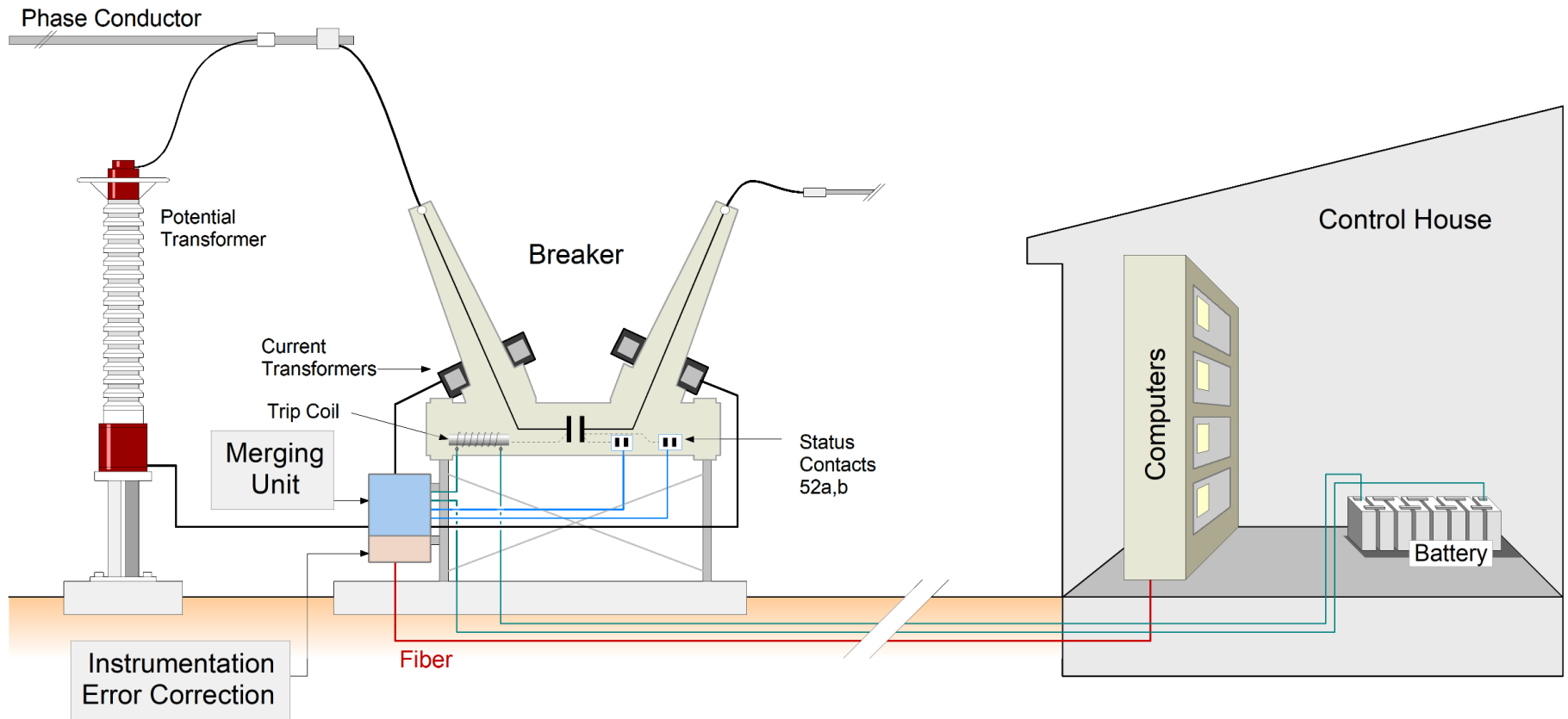
## Error Correction Performance



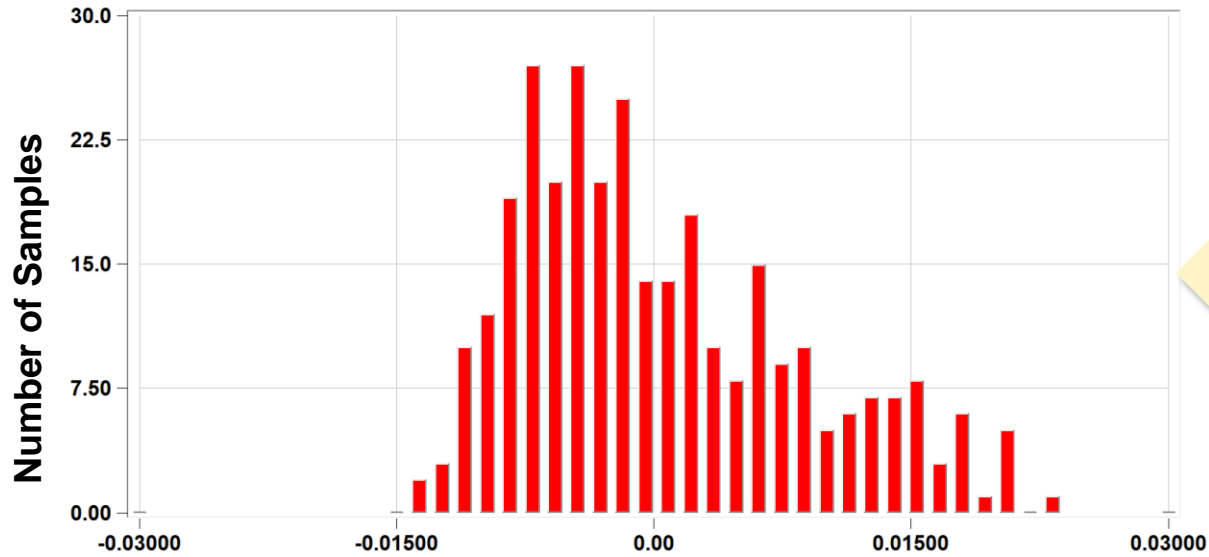
Estimated results match actual primary current with less than 1% error

# Intelligent Merging Units Provide Corrected Primary Values

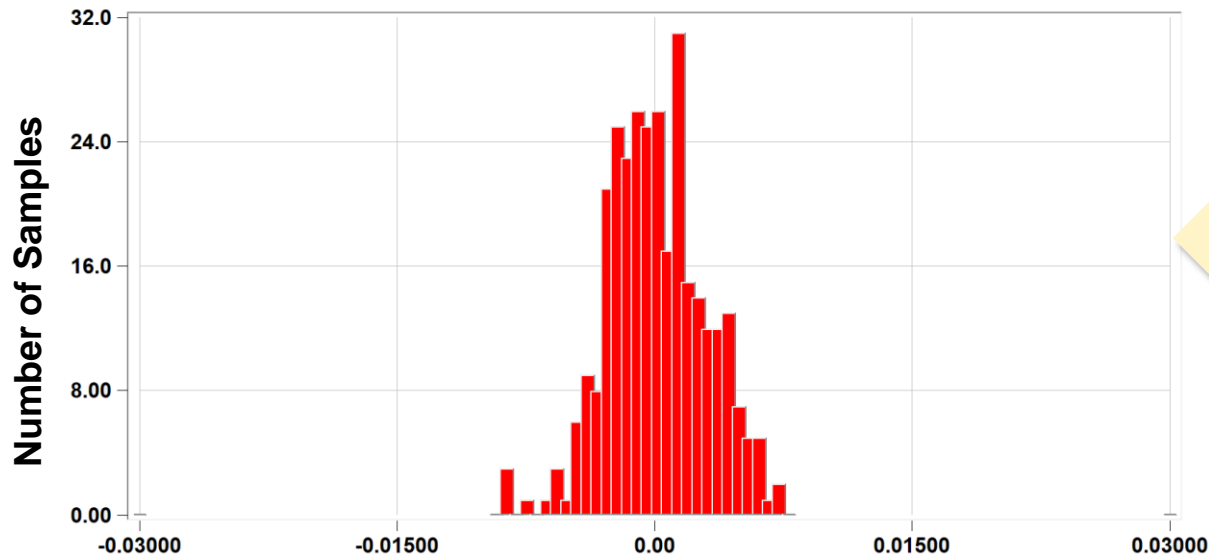
Error Correction Integrated into Merging Units  
(alternative: in substation computers)



# Residual Analysis with/without Instrumentation Error Correction



Histogram of Residuals without Correction (300 SE Executions)



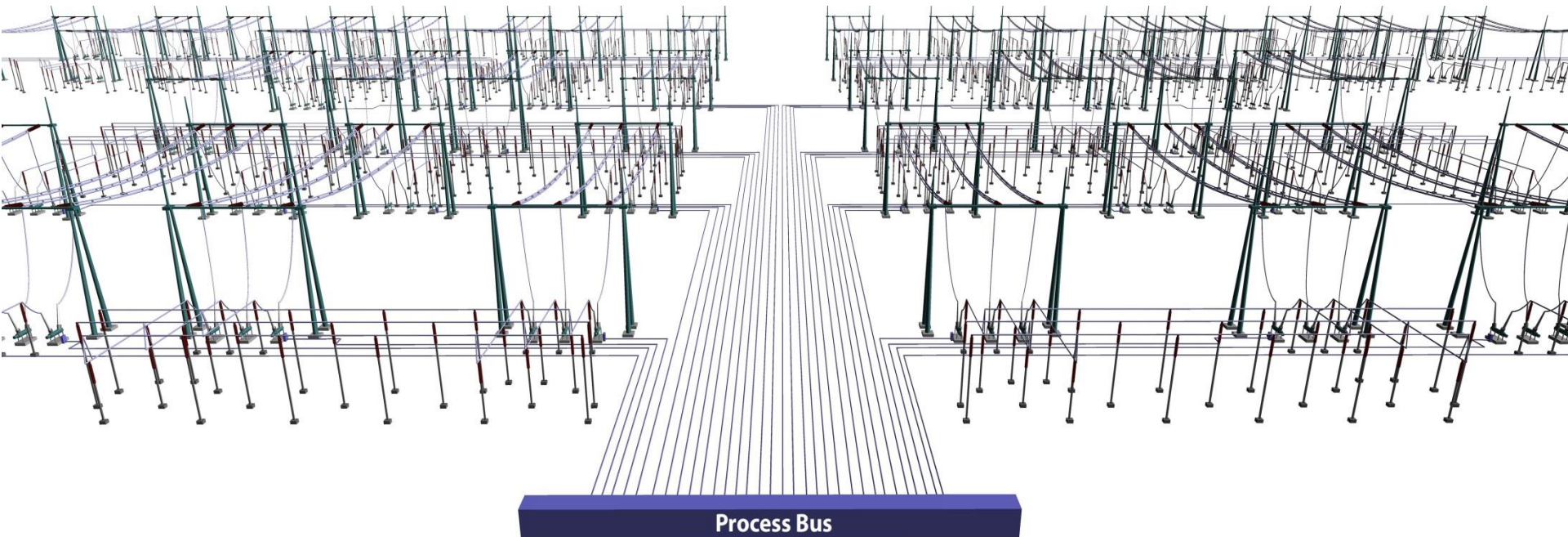
Histogram of Residuals with Correction (300 SE Executions)

Normalized Error

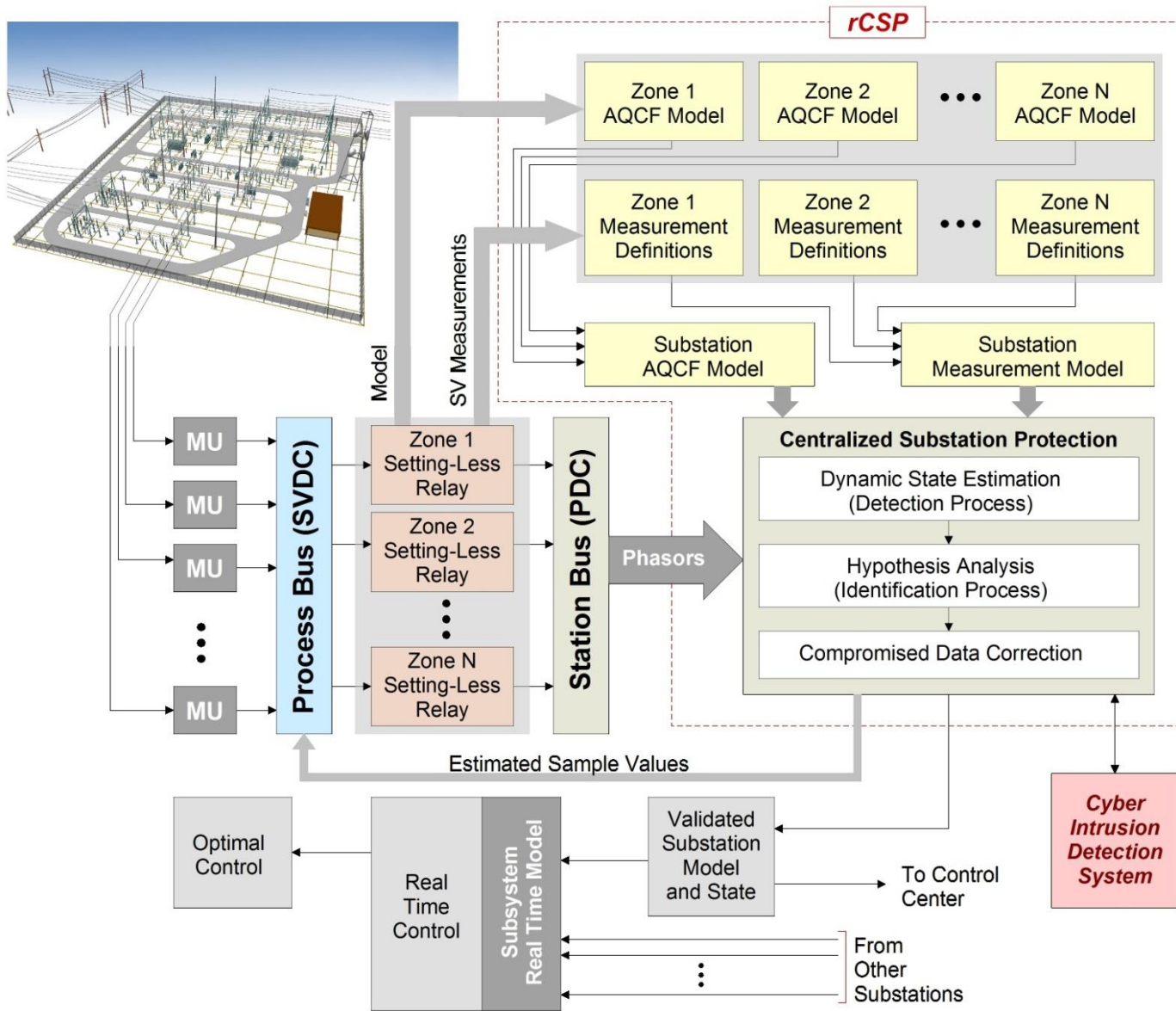
# The Future

## The Digital Substation

### Integration of Protection and State Estimation



# Dynamic State Estimation Based Centralized Protection Scheme



## Resilient Centralized Substation Protection (rCSP)

# Concluding Remarks

IEEE and CIGRE Efforts Move Towards the DIGITAL SUBSTATION.

**Resiliency:** The entire process should be automated with self healing capabilities against data errors, hidden failures and cyber attacks.

**Awareness:** Automatic provision of substation dynamic state.

**Asset Management:** Automated testing and in-line testing of active substation protection and control systems.